DIVISION RINGS SATISFYING A GENERALIZED POLYNOMIAL IDENTITY WITH AN ANTI-AUTOMORPHISM

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ABSTRACT. Let D be a division ring with center F and $\star$ be an F-anti-automorphism of D. In [7], the authors proved that if D satisfies a non-trivial generalized polynomial identity, then D is a finite dimensional vector space over F. In this paper, we shall extend this result for a division ring satisfying a σ^m-generalized rational identity, where m is a positive integer.

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